

Name _____ School _____ Grade _____

- 1) Let A, B, and C be digits in base 7, with possible values 0, 1, ..., 6. If $ACB_7 + BCC_7 = 1400_7$, what is the base 10 value of ACB_7 ?
- 2) Find the solution set for the inequality: $\frac{1}{x} + 2x \geq 3$.
- 3) A triangle has a right angle at A with $AC = 3$ and $AB = 1$. The angle bisector at B meets AC at P. What is the length of CP?
- 4) A function f satisfies $f(0) = 0$, $f(2n) = f(n)$, $f(2n + 1) = f(n) + 1$ for all positive integers n . What is the value of $f(2017)$?
- 5) A cube of cheese $c = \{(x, y, z) | 0 \leq x, y, z \leq 1\}$ is cut along the planes $x = y$, $y = z$, and $x = z$. How many pieces are there?
- 6) What is the area of a triangle with sides 10, 10, 16?
- 7) A rectangle is inscribed in a quarter-circle of radius 6, as shown, so that The sum of the width and height is 8. What is the area of the rectangle?



Answers		
1)	2)	3)
4)	5)	6)
7)	8)	9)
10)	11)	12)

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- 13 Compute the least possible, non-zero value of $A^2 + B^2 + C^2$ such that A, B, and C are integers satisfying $A \log 16 + B \log 18 + C \log 24 = 0$.
- 14) How many ordered pairs (x, y) of integers (not necessarily positive) satisfy $\frac{1}{x} + \frac{1}{y} = \frac{1}{4}$?
- 15) What is the smallest integer larger than $(\sqrt{5} + \sqrt{3})^6$?
- 16) The magic square shown uses each integer from 1 through 9, exactly once, so that The sum along any row, column, and both diagonals is 15. What is the value of x?
- | | | |
|---|---|---|
| | 9 | 4 |
| x | | |
| | | |
- 17) The price of a shirt is increased 25%, and then there is another increase of 20%. What is the overall percentage increase?
- 18) In this addition example, $AA + BB + CC = BAC$ different letters represent different digits. What is the value of the three-digit number BAC?
- 19) There are 10 Bluray's in a package. Mike reads the front of the package and realizes that 3 of the Bluray's are ones he likes. If he selects 4 at random, what is the probability that he gets exactly two of the ones he likes?
- 20) If $\sin x + \cos x = \sin x \cos x$, then what is $\sin x \cos x$?
- 21) If $f(x) = x^2 + 1$, what is the value of $f(f(f(f(0))))$?
- 22) If a and b are positive real numbers satisfying $(a - b)^2 = 4(ab)^3$, what is the smallest possible value of $\frac{1}{a} + \frac{1}{b}$?
- 23) Triangle ABC has $AB = 6$, $AC = 5$ and $BC = 4$. Points P_1, P_2 , and P_3 on BC satisfy $BP_1 = BP_2 = BP_3 = P_3C = 1$. What is the value of $(AP_1)^2 + (AP_2)^2 + (AP_3)^2$?
- 24) Compute the largest of the three prime divisors of $13^3 + 16^5 - 172^2$.

Answers		
13)	14)	15)
16)	17)	18)
19)	20)	21)
22)	23)	24)

